

**MATH 435**  
**Spring 2009**

**Homework #6**  
**Prof. Biswa Nath Datta**

1. (a) Determine an upper bound on the error for Euler's Method to solve the IVP:

$$y' = -6xy, \quad y(0) = 7$$

from  $x = 0$  to  $x = 1$ , with  $h = 0.25$ .

- (b) Solve the above equation at  $x = 1$  using Euler's Method.

- (c) Compare the bound obtained in (a) with the actual error obtained from (b).  
(Exact solution is  $y(x) = 7e^{-3x^2}$ ).

2. Derive the following predictor-corrector formula:

$$y_1^{(0)} = y_0 + hf(t_0, y_0)$$

$$y_{i+1}^{(k)} = y_i + \frac{h}{2}[f(t_i, y_i) + f(t_{i+1}, y_{i+1}^{(k-1)})], \quad k = 1, 2, \dots$$

Apply this formula to obtain an approximation of  $y(0.2)$  of the IVP:  $y' = t - \frac{1}{y}$ ,  $y(0) = 1$ ,  $h = 0.1$  with four digits accuracy.

3. Given

$$y' = -y^2$$

$$y(1) = 1$$

$$\text{and } h = 0.1$$

Apply Four-Step Adams-Bashforth formula to compute  $y(1.4)$ ,  $y(1.5)$  and  $y(1.6)$ .  
Tabulate the results with approximate and exact values and errors.

**(Exact solution:**  $y(t) = \frac{1}{t}$ )